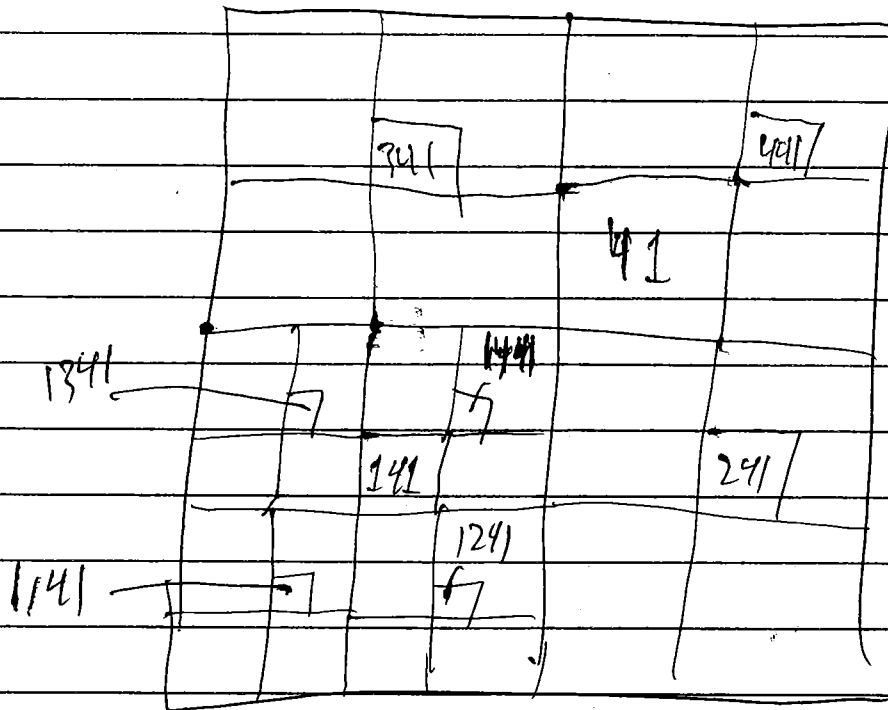


Sept 13

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41 is empty implies that 141, 241, 341, and 441 are empty

For a point to be in square 241, the previous point must have been in square 41, and T_2 applied.

Every ~~square~~ square with address containing the address of an empty square must itself be empty.

$$T_1(x, y) = (x/2, y/2)$$

$$T_2(x, y) = (x/2, y/2) + (1/2, 0)$$

$$(12)^\infty = (x_a, y_a) \quad (21)^\infty = (x_b, y_b)$$

$T_2(x_a, y_a)$ has address $212121212 \dots$

$T_1 T_2(x_a, y_a)$ has address $1212121212 \dots (12)^\infty$

That is $T_1 T_2(x_a, y_a) = (x_a, y_a)$

$$\begin{aligned} T_2(x_a, y_a) &= (x_a/2, y_a/2) + (1/2, 0) \\ &= (x_a/2 + 1/2, y_a/2) \end{aligned}$$

$$\begin{aligned} T_1 T_2(x_a, y_a) &= T_1(x_a/2 + 1/2, y_a/2) \\ &= (x_a/4 + 1/4, y_a/4) \end{aligned}$$

Because $T_1 T_2(x_a, y_a) = (x_a, y_a)$, we have

$$(x_a/4 + 1/4, y_a/4) = (x_a, y_a)$$

$$y_a/4 = y_a \text{ means } y_a = 0$$

$$x_a/4 + 1/4 = x_a$$

$$1/4 = x_a - x_a/4 = \frac{3}{4} x_a$$

$$\frac{1}{3} = \frac{4}{3} \cdot \frac{1}{4} = x_a$$