

Both Julia sets and the Mandelbrot set are generated by iterating

$$z_{n+1} = z_n^2 + c$$

where  $z_n, z_{n+1}$ , and  $c$  are complex numbers.

Writing  $z_n = x_n + iy_n$

$$z_{n+1} = x_{n+1} + iy_{n+1}$$

$$c = a + ib$$

Then  $z_{n+1} = z_n^2 + c$  becomes

$$x_{n+1} = x_n^2 - y_n^2 + a$$

$$y_{n+1} = 2x_n y_n + b$$

For each complex number  $c$ , there is a Julia set,  $K_c$

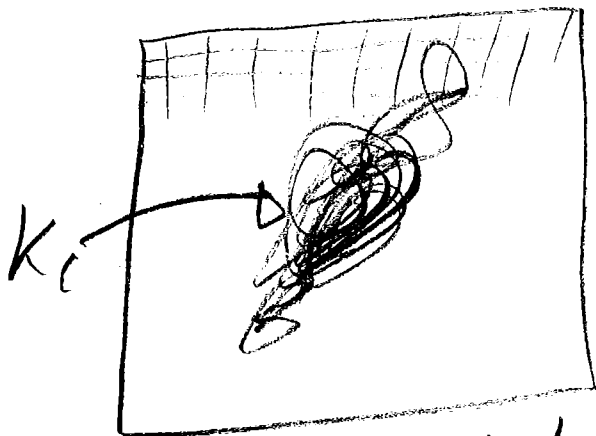
For each pixel, the center is  $z_0$ . Generate

$$z_1 = z_0^2 + c$$

$$z_2 = z_1^2 + c$$

$\vdots$

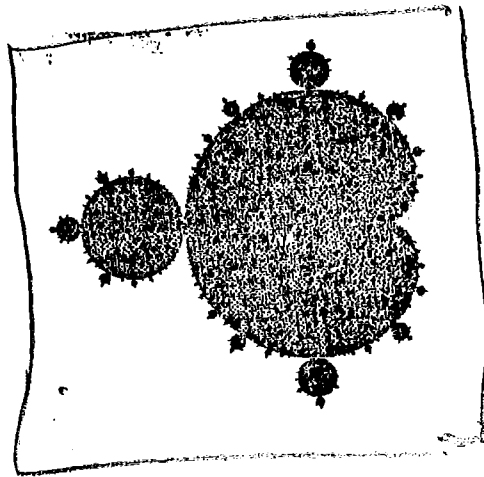
$$z_N = z_{N-1}^2 + c$$



$z_0$  values

If all  $z_1, z_2, \dots, z_N$  lie within a distance of 2 from the origin,  $z_0$  belongs to  $K_c$ .

For the Mandelbrot set, each pixel corresponds to a  $c$  value. For each  $c$ , begin the iteration with  $z_0 = 0$ , and compute  $z_1 = z_0^2 + c$ ,  $z_2 = z_1^2 + c, \dots$   
 $z_N = (z_{N-1})^2 + c$ . If all  $z_1, z_2, \dots, z_N$  lie within a distance of 2 from the origin,  $c$  belongs to  $M$ .



$c$  values