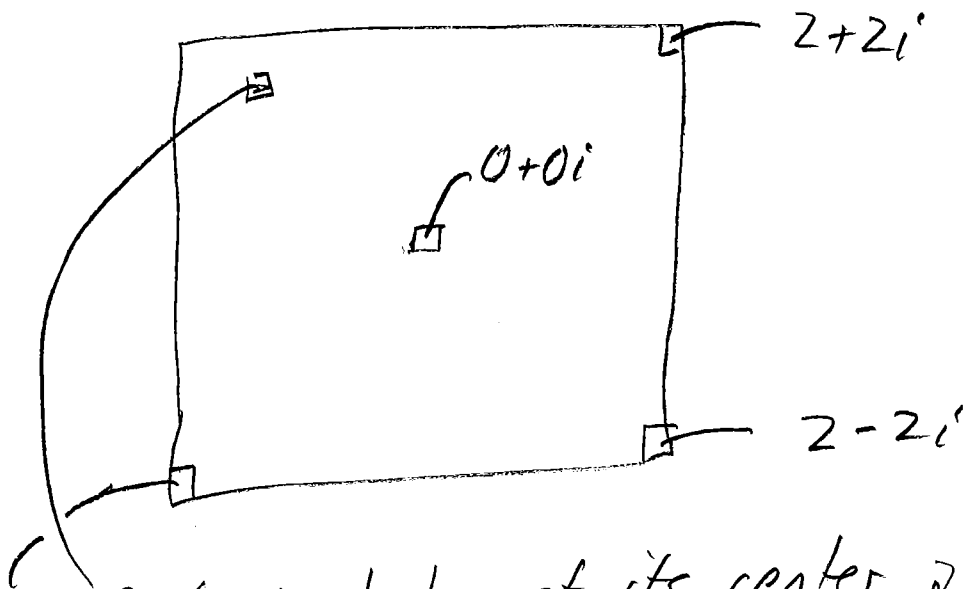


Julia sets: fix the number  $c$

Nov 27 notes



$-2-2i$  Each pixel has at its center a  $z_0$  value

For each  $z_0$ , iterate

$$z_1 = z_0^2 + c$$

$$z_2 = z_1^2 + c$$

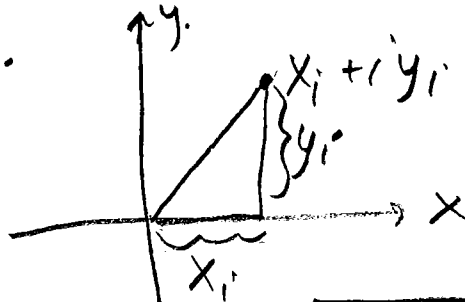
$$z_3 = z_2^2 + c$$

$\vdots$

$$z_N = z_{N-1}^2 + c$$

$N = \text{max. number of iterates}$

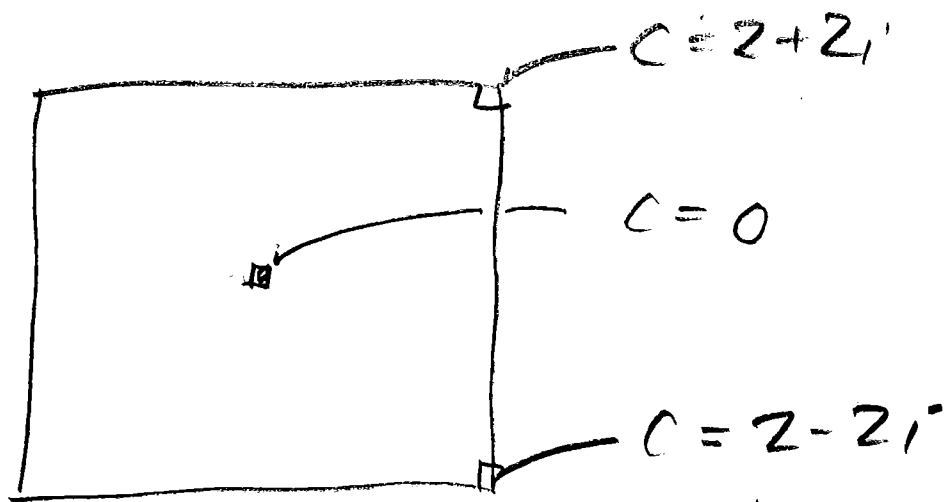
$$z_i = x_i + iy_i$$



dist. to origin is  $\sqrt{x_i^2 + y_i^2}$

IF dist to origin,  $\sqrt{x_i^2 + y_i^2}$  is greater than 2, then  $\text{dist}^2 = x_i^2 + y_i^2$  is greater than 4.

IF no  $z_i$  is farther than 2 from the origin,  $z_0$  belongs to the Julia set.



For each  $c$ , start with  $z_0 = 0$  and iterate  $z_1 = z_0^2 + c$ ,  $z_2 = z_1^2 + c$ , ...  
 $z_N = z_{N-1}^2 + c$ . The Mandelbrot set is those  $c$  for which the iterates remain closer than 2 to the origin.  
 The Mandelbrot set also is those  $c$  values for which the Julia set is connected.